Real-time digital simulation-based modeling of a single-phase single-stage PV system

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A R T I C L E   I N F O

Article history:
Received 2 December 2014
Received in revised form 29 January 2015
Accepted 30 January 2015

Keywords:
Incremental conductance (IC)
Real-time laboratory (RT-LAB)
Maximum power point tracking (MPPT)
Proportional resonant (PR) controller
Single-phase single-stage PV
Discrete models

A B S T R A C T

This paper presents real-time digital simulation-based modeling of a single-phase single-stage PV system. Discrete models of voltage source converter (VSC) controls, including proportional resonant (PR) current control and phase-locked-loop (PLL) are developed in RT-LAB. An improved incremental conductance-based maximum power point tracking (MPPT) method that can mitigate error signal spikes is proposed and modeled in RT-LAB as well. Simulation results demonstrate the faster response of the proposed MPPT and the real-time simulation performance of the developed system model.

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1. Introduction

Photovoltaic (PV) is considered as a widely spread source of renewable energy due to its low operational cost, low maintenance cost, and most importantly for being environment friendly without pollution. According to the literature, PV cells will become the most important alternative renewable energy sources till 2040 [1–5].

Real-time digital simulation based high-fidelity modeling can give a close-to-reality representation of the system dynamic performance. In addition, real-time simulation speed can be reached. Such simulation model can be used for prototype operation and control tests.

Modeling PV systems in real-time digital simulation has been mentioned in Ref. [6] where a PV serving a load through a dc/dc converter is modeled and simulated in RTDS. In another paper [7], a PV cell, its dc-link capacitor and a dc chopper are modeled in RT-LAB while the physical controller for the chopper is integrated into the software simulation model through RT-LAB interface. A grid-connected PV system has a more complicated control system. Modeling of such a system has not been seen in the literature. The objective of this paper is to model a single-phase single-stage PV system in RT-LAB.

Control of the interfacing dc/ac converter, including PR current control, PLL and MPPT will all be modeled in RT-LAB. In addition, an improved MPPT will be proposed and modeled in this paper. Various types of MPPT algorithms have been proposed in the recent years, e.g., hill climbing (HC) [8,9], perturb and observe (PO) [10–13], and incremental conductance (IC) [14,15]. Among these types of algorithms, HC and PO are two commonly used approaches because of their simple control structures. The disadvantages related to these methods are: increased losses at steady state due to large perturbation around maximum power point; reduced dynamic performance the dynamic behavior when there is a sudden change in irradiance or at any other sudden dynamic event [16–18]; and large oscillations around the maximum point [19].

On the other hand, IC methods are based on the fact that the slope of the PV array power curve versus voltage is zero at the maximum power point (MPP). IC method has a lot of advantages compared with PO method. It can exactly determine when the MPP is reached. In a PO method, there are oscillations around the MPP. Accuracy of the IC method in tracking the maximum power or responding to the irradiance changes is more than that of a PO method [16,17]. Less ripples in output power are experienced during the operation compared with PO method [19]. And finally dynamic behavior of the IC based methods are faster when an operating point change is applied to the system [19].

Complexity of the IC method has limited the widespread implementation of this algorithm [17]. In the literature many researchers have focused on improving the dynamic response and steady state accuracy of the IC method [19–23]. In Ref. [19], it is demonstrated that the dynamic response of the IC method can be greatly improved if a proportional integral (PI) controller is used.
Moreover, if the output of the PI controller aims to modify the PV current instead of the PV inverter’s duty cycle, the dynamic response is even better. A variable step-size IC MPPT is proposed in [24]. The step size is automatically adjusted according to the derivative of power to voltage (\( \frac{dP}{dV} \)) of a PV array. The step size will become tiny as becomes very small around the MPP. Thus, it provides a very good accuracy at steady state and the dynamics of the MPPT will be improved. However, the proposed method has added more complexity to the IC algorithm.

In this paper, a new algorithm is proposed which can improve the steady-state response and dynamic behavior of MPPT. In the proposed method, instead of using the traditional incremental error (\( \frac{dI}{dV} + \frac{dV}{dV} \)) which could lead to spikes when \( dV \) is approaching zero, the proposed error will no longer contain \( dV \) at the denominator. This approach will remove the conditional statements from the IC-PI MPPT and lead to improvement in dynamic performance of the MPPT algorithm. The designed algorithm provides no oscillations around MPP (which was one of the main drawbacks of MPPT algorithms), and it can reach to the MPP very fast. Moreover, as the proposed algorithm is simple, it is easy to be implemented in real-time MPPT controller. Better efficiency, less calculation time and memory allocation compared to traditional algorithms can be achieved.

The rest of the paper is organized as follows: the system configuration will be described in Section 2. PV control models in RT-LAB, which consist of a PR controller and MPPT, are described in Section 3. Case studies are presented in Section 4. Section 5 presents the conclusion.

2. System configuration

The PV system configuration is illustrated in Fig. 1. The model is composed of a PV array, a dc/ac inverter, and a filter. The PV array is composed of a number of parallel connected PV strings. These PV strings consist of a number of serially connected PV cells. Parameters of these cells will be different for different commercial PV models. Each cell in a module can be modeled as a photo-generated current source in parallel with a diode and a shunt resistor, \( R_p \), as well as in series with a series resistor, \( R_s \) as shown in Fig. 1.

\[ I_{ph} = A_{ph} \cdot I_{sc} \cdot E_z \]  

(1)

where \( E_z \) is the effective sun radiance considering the effect of incidence angles, transmission through glass, encapsulant and spectral responses of the cell. \( A_{ph} \) is the proportionality factor which is related to the cell temperature and is usually close to one. Current through the diode can be represented by the Shockley equation in the following [25]:

\[ I_{diode} = I_{sat} e^{\frac{V_{ph} - V_{ph} \cdot R_s}{m \cdot V_T}} \]  

(2)

where \( I_{sat} \) is the diode saturation current which strongly depends on the cell temperature. Cell voltage and current are noted as \( V_{PV} \) and \( I_{PV} \) respectively. \( m \) is the diode factor, a measure of ideality of the diode, usually a number between 1 and 2. In situations where the PV array is modeled by two parallel diodes, \( m \) is set to 1, the ideal factor.

\[ V_I = \frac{k \cdot T_{cell}}{q} \]  

(3)

3. PV control

The main block diagram of the PV control is illustrated in Fig. 2. The inputs of the MPPT block are the measurements from the PV array (\( I_{PV}, V_{PV} \)). The output of the MPPT block is then modified to shape the reference PV AC current magnitude. The measured AC current of the grid is then compared with the reference signal and the error will be sent to the proportional resonance (PR) controller. The output of the PR controller is then sent to the PWM block to generate the pulses for the PV inverter. A single-phase phase-locked-loop (PLL) is used to synchronize the PV reference current with the AC grid in Fig. 2.

Since the real-time simulators are working in discrete time domain, all the controllers are modeled in discrete time domain. Detailed parameters of the PLL, the MPPT, and the PR controller are given in Table 1.

![Fig. 1. Topology of a single-phase PV grid integration system. \( L_g = 10 \text{ mH}, L_p = 20 \text{ mH}, C_f = 10 \mu F, V_{gf} = 230 \text{ V}. \) Sunpower PV panel: \( V_{PV} = 440 \text{ V}, P_{PV} = 2.45 \text{ kW}. \)](image)

![Fig. 2. Block diagram of PV control system.](image)
Table 1
Parameters of single phase PV for Sunpower Panel.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal voltage</td>
<td>440 V</td>
</tr>
<tr>
<td>Open circuit voltage per cell</td>
<td>64.2 V</td>
</tr>
<tr>
<td>Short circuit current per cell</td>
<td>5.96 A</td>
</tr>
<tr>
<td>$K_p, K_c$ of PR controller</td>
<td>100, 500</td>
</tr>
<tr>
<td>$\omega$</td>
<td>377 rad/s</td>
</tr>
<tr>
<td>$K_p, K_c$ of MPPT controller</td>
<td>5, 20</td>
</tr>
<tr>
<td>$L_p, L_c$ of AC filter</td>
<td>180, 3200</td>
</tr>
<tr>
<td>$L_c$ of AC filter</td>
<td>20, 10 mH</td>
</tr>
<tr>
<td>$C$ of AC filter</td>
<td>1 µF</td>
</tr>
<tr>
<td>Frequency</td>
<td>60 Hz</td>
</tr>
</tbody>
</table>

3.1. Discrete time single phase PLL

The main task of phaselocked-loop (PLL) is to provide a reference phase signal synchronized with the AC systems. The reference phase is then used to generate a carrier waveform for firing pulses in control circuits of converters. PLL has the capability to dynamically change the reference phase due to any dynamic change in AC systems, ensuring synchronization of the converter’s output with the AC system.

The PLL model in Simpower systems was developed by Pierre Giroux in 2007. Description of the PLL models can also be found in [26]. The continuous time PLL model will be converted to a model in discrete time. The main block diagram of the discrete time PLL is illustrated in Fig. 3, derived based on Fig. 2.

The input of the PLL is the grid AC voltage, $v_gf$, and the output is the frequency or angle which is synchronized with the grid. Furthermore, there is a variable frequency mean value calculator represented by a simple integrator and a delay block. Suppose $v_gf$ is sinusoidal and can be expressed as $v_gf = V_gf \sin \theta_g$. Then multiplied by $\cos \theta$, we have

$$V_q = \frac{1}{2} V_gf(\sin(\theta_g + \theta) + \sin(\theta_g - \theta)).$$

(4)

There are two components in $V_q$, one is of high frequency and the other will be a low frequency one. If the angular speeds of $\theta_g$ and $\theta$ match each other, then the second component is a dc value. After passing the integrator, the effect will be mainly due to the second component as the integration of the high-frequency component will be around zero. The objective of the PI controller will bring the second component in $V_q$ to zero, i.e., $\theta_g = \theta$. Thus, PLL can obtain the angle of $v_gf$. The frequency of the grid voltage can also be obtained.

3.2. Discrete proportional resonant (PR) controller

A PR controller provides an infinite gain in a very narrow bandwidth that is centered at the resonance frequency ($\omega$). As a result, steady-state error is eliminated at the resonance frequency $\omega$. Therefore, a PR controller can track a sinusoidal reference signal. For a single-phase PV converter, the error signal is the mismatch of the grid AC reference current and measured grid instantaneous current. The general control block of the PR controller is illustrated in Fig. 4.

The Bode plots of a PR controller with different resonance gains are illustrated in Fig. 5. It can be observed that at frequencies close to 377 rad/s or 60 Hz, the PR controller’s gain is very large. This in turn will cause the gain of the close-loop system very small at this frequency. Therefore, steady-state error at $\omega$ will approach zero. In this study, the PR controller for the single-phase PV has been designed to compensate the high order frequencies of: 3rd, 5th, 7th, and 9th.

The PR controller will be modeled in discrete time for RT-LAB. The original system can be expressed as follows.

$$y(s) = \frac{K_p \epsilon(s) + K_c}{s^2 + \omega^2} \frac{K_c \epsilon(s)}{y_2(s)}$$

(5)

The proportional block will be kept the same in the discrete domain. In contrast, converting $y_2(s)$ into discrete form requires derivation. The procedure can be found in Ref. [27] and also described as follows. Rearranging $y_2(s)$ will lead to:

$$y_2(s) = \frac{K_p}{s^2 + \omega^2} \epsilon(s)$$

$$\frac{s^2 + \omega^2}{s^2} y_2(s) = \frac{K_c}{s} \epsilon(s)$$

(6)

$$\frac{y_2(s)}{\omega^2} + \frac{\omega^2}{s^2} y_2(s) = \frac{K_c}{s} \epsilon(s)$$

$$\frac{y_2(s)}{\omega^2} = \frac{1}{\omega^2} \left[ K_c \epsilon(s) - \frac{1}{\omega^2} \omega^2 y_2(s) \right].$$
Defining a new variable \( z \), the simplified model of \( y_2(s) \) is expressed by:

\[
\begin{align*}
y_2(s) &= \frac{1}{s} \left[ K_c \varepsilon(s) - z(s) \right] \\
z(s) &= \frac{1}{s} \omega^2 y_2(s).
\end{align*}
\]

Discretizing (7) is now limited to an integrator which should be changed from s-domain into discrete time integrator, where \( 1/s \) corresponds to \( \frac{1}{T_s} \). The block diagram of the proposed controller has been illustrated in Fig. 6, but due to the space limitations, only the first harmonic has been shown here.

The PR controller aims to control the grid side AC current. To achieve this objective, the error of the reference PV current and measured PV current will be used as the input for the PR controller. The reference current magnitude generated from the output of the MPPT block will be synchronized with the grid voltage before sending to the PR controller. The synchronization steps will be carried out in a single-phase PLL block. The output of the PR controller is the voltage reference which will be directly sent to the pulse width modulation (PWM) generation unit.

### 3.3. MPPT for PV systems

The MPPT is the main part in the photovoltaic systems which can ensure the maximum captured power from the PV array. It continuously tunes the system regardless of weather or load condition change such as: irradiance change, ambient temperature, or wind which can affect the PV array output. Conventional MPPT algorithms use \( \frac{dP}{dV} = 0 \) to ensure the maximum power harvest.

#### 3.3.1. Traditional IC method

The incremental conductance technique has been implemented here which directly focuses on power variations. It means the power slope of the PV is zero at MPP (\( \frac{dP}{dV} = 0 \)), positive in the left hand side of MPP and negative in the right hand side. The output current and voltage of the PV panel are used to calculate the conductance and incremental conductance. The basic approach is to compare the conductance (\( I/V \)) with the incremental conductance (\( dI/dV \)) and decide when to increase or decrease the PV voltage. In order to reach the maximum power point, the derivative of the power (\( dP/dV \)) should be always zero. Considering \( P = V \cdot I \) [17]:

\[
\frac{dP}{dV} = \frac{d(V \cdot I)}{dV} = I + V \frac{dI}{dV} = 0
\]

\[
\Rightarrow \frac{dI}{dV} = -\frac{I}{V}
\]

which means when the conductance is opposite of the incremental conductance, the maximum power is guaranteed.

The discrete real-time traditional IC MPPT model is shown in Fig. 7. The conductance will be added to the incremental conductance to generate an error signal. The objective of the PI controller is to make the error signal approach zero. For real-time simulations of IC, the output of the MPPT is directly sent to the current controller loop to take the advantage of the fast response of the current controller loop. Here the output of the MPPT block will be added to a constant (PV power divided by the grid voltage RMS) to form the magnitude of reference current value. This current reference will be used in the current control to adjust the grid current by means of a PR controller. A dead band is used to at \( dV = 0 \) conditions. If \( dV \) becomes zero, the error will be infinity and the proposed MPPT algorithm will not work properly. The traditional dead-band controller in Fig. 7 shows that if \( dV = 0 \), a very small value is considered \( (1 \times 10^{-6}) \) to avoid the error to be infinity. The problem with traditional dead-band controller is that even the value of \( dV \) is set to a small value, large spikes in the output of MPPT will appear when \( dV \) is oscillating around zero. This is not acceptable for the controller.

**MPPT mechanism** Fig. 8 shows the sample \( V-I \) characteristic of a PV. Suppose the operating point is at Point 1 where the error is greater than zero. According to the MPPT in Fig. 7, the output of the PI unit will increase, which in turn leads to the decrease in the AC current reference. The grid voltage is constant. In addition, the current control response is much faster than MPPT and the current is synchronized with the grid voltage through PLL. Therefore, this leads to the reduction in active power at the AC side. Ignore the loss of the switches, the average power at the dc side should be the same of that at the ac side. Therefore, at the dc side of the converter, if we assume that the dc voltage \( V_{PV} \) is kept the same, then the dc current \( I_{PV} \) will have a reduction due to the reduction in the AC current magnitude. Reduction in \( I_{PV} \) will lead to increase in \( V_{PV} \) and \( P_{PV} \). Until the error reaches zero, the PI control will keep adjusting the AC current reference.

Similarly, when the PV system is at Point 3 where the error is less than zero, then the AC current reference will have an increase, which in turn leads to the increase in \( I_{PV} \) and the reduction in \( V_{PV} \). The combination leads to the increase in \( P_{PV} \). It is possible to have oscillations in power if the gains of the PI controller are large. This can lead to too much increase in the AC current reference and \( I_{PV} \). At that point, the error signal becomes greater than zero. The AC
current reference then will see a reduction, so on and so forth till the error approaches zero.

3.3.2. Modified IC-PI MPPT

For traditional IC-PI MPPT, when \( dV \) reaches to zero, the error signal will go to infinity and the output of the MPPT will have a spike. To solve e problem, the proposed algorithm suggests that the \( dV \) should be removed from the denominator of the error signal. Modified error signal can be considered as: \( V \cdot \frac{dI}{dV} + I \cdot \frac{dV}{V} \), which can be viewed as the previous error signal \( \frac{dI}{V} \) multiplied by \( V \cdot \frac{dV}{V} \).

In this case, \( dV \) is no longer in the denominator and it will not cause any spikes in MPPT output even when \( dV \) is zero. However, the error signal should provide the same implication of operation point position as the previous error signal. Modification is presented as follows.

Analysis of the error signal used in traditional IC is presented as follows.

If \( \text{error} > 0 \) \( \left( \frac{dI}{dV} > -\frac{I}{V} \right) \) \( \Rightarrow \begin{cases} dV > 0 \Rightarrow VdI + ldV > 0 \\ dV < 0 \Rightarrow VdI + ldV < 0 \end{cases} \) (10)

Eq. (10) shows that if the traditional error is positive, the sign of the proposed new error will depend on the sign of \( dV \). If \( dV \) is positive, the defined new error will be positive, same as the traditional error; but if \( dV \) is negative, the proposed new error will be

Fig. 9. Improved IC MPPT for PV systems.

Fig. 10. \( V-I \) and \( P-V \) curves for different irradiance values of Sunpower PV panel.

Fig. 11. Irradiance step change and the MPPT input error.

Fig. 12. The AC current magnitude reference.

Fig. 13. PV output power and dc current for traditional MPPT.
negative, which is a contradiction. Same thing happens when the error is negative:

$$f_{\text{error}} < 0 \quad \left( \frac{dI}{dV} < \frac{1}{V} \right) \Rightarrow \begin{cases} dv > 0 & \Rightarrow VdI + IdV < 0 \\ dv < 0 & \Rightarrow VdI + IdV > 0 \end{cases}$$ (11)

Therefore, a modification can be proposed to ensure the modified error signal having the same implication of operation point as the traditional error signal.

The new error is now multiplied by the sign of $dV$. The sign of the new error will always agree with the sign of the traditional error. The proposed error is very small compared with traditional error signal, which justifies a large gain ($K = 1000$) before applying this error to a discrete PI controller. The improved MPPT algorithm is illustrated in Fig. 9. As it can be seen, the error signal will be magnified by a gain, then the output will be sent to the PI controller.

4. Case studies

This section is dedicated to real-time simulation results which have been conducted in real-time digital simulator RT-LAB. A real PV model named as Sunpower SPR 305 WHT is considered for verification of the proposed algorithm for IC-PI MPPT method. The PV model is composed of 96 cells combined in 8 series PV strings. For this type of PV panels, $I_{\text{ph}}$ equals to 5.96 A, $R_p = 900 \, \Omega$ and $R_s = 0.038 \, \Omega$. The $V-I$ and $P-V$ curves for different irradiance values have been illustrated in Fig. 10.

Different irradiance values will provide different $V-I$ curves. For $1 \, \text{kW/m}^2$, the maximum power will be around $2.45 \, \text{kW}$ when the voltage is $440 \, \text{V}$. For the dynamic event, a step change to the irradiance is applied by decreasing the irradiance at $t = 21 \, \text{s}$ from $1 \, \text{kW/m}^2$ to $0.75 \, \text{kW/m}^2$. Such a step change is illustrated in Fig. 11.

The input error for MPPT controller for both algorithms has also been shown in Fig. 11. It shows that the traditional method is suffering from a lot of spikes during the simulation because the error is oscillating around zero which makes the dead-band controller to act. In contrast, the proposed algorithm provides no spikes.

The AC current magnitude reference $I_{\text{ref}}$ is plotted in Fig. 12 for both traditional MPPT and proposed MPPT. It can be observed that the proposed MPPT results in a much smoother $I_{\text{ref}}$.

Simulation results of the PV output power and current following the applied irradiance change are illustrated in Figs. 13 and 14. As it can be observed, after the sudden irradiance change, the traditional IC-PI method will face a lot of dynamics and it takes a long time for the active power to be settled to its new reference value. In contrast, the proposed IC method can respond to the sudden dynamic event very fast and it will be settled to the new reference value shortly.

The dc voltage is shown in Fig. 15. As the irradiance is changed at $21 \, \text{s}$, the maximum power is then set to the new value and referring to the $V-I$ characteristic presented in Fig. 10, the output voltage will be set to the new value (425 V), which is less than the previous value. Compared with the traditional method, the proposed method can fix the voltage to the new set-point very fast and without much dynamics.

Results of operating point change have shown a great improvement in the MPPT algorithm. The proposed algorithm is not only easy to be implemented but also provides a faster response and improved dynamic performance of the PV energy systems.

4.1. RT-LAB performance

To examine the performance of real-time simulators, the performance metrics of the model are extracted through Opmonitor Block in the RT-LAB. Opmonitor block provides necessary information regarding the performance or RT-LAB. It mainly records computation time, step size, idle time, and number of overruns. Computation time is the time spent in calculation of the previous step time excluding the communication overhead in $\mu$s. Step size clarifies the real step size which has been selected for the model during the run which is $25 \, \mu$s in this study. Idle time is the idle time during the execution of previous time step. Idle time plus computation time should be equal to the real step size. Number of overruns is the number of overruns during the run which is zero in this case clarifying the stable condition of running. The results of the Opmonitor Block are included in Fig. 16. In this case study, the computation time is less than 1 microsecond which clarifies the CPU usage of the model less than 4% ($\frac{25 	imes 24}{25} \times 100$%), which is a great performance.
Furthermore, there is no overrun detected by the simulator which means all the cores are performing in a balanced manner.

5. Conclusion

This paper presents real-time digital simulation-based modeling of a single-phase single-stage PV grid integration system. Models for the PV panel, PLL, PR current control and MPPT are all developed in discrete domain. In addition, an improved MPPT algorithm is proposed this paper. The proposed MPPT algorithm does not need dead-band blocks used in traditional IC MPPT control. Simulation case studies demonstrate that the proposed MPPT has a superior performance than the traditional MPPT.

Acknowledgements

This research is supported in part by Duke Energy through Community Power System Simulation project. The authors acknowledge OPAL-RT for support in RT-LAB setup.

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